

Exam. Code : 121203
Subject Code : 502192

B.A./B.Sc. 3rd Semester (Batch 2024-27/28) (CBGS)

MATHEMATICS
(Differential Equations)

Time Allowed—3 Hours]

[Maximum Marks—100

Note :— Attempt FIVE questions in all, selecting at least ONE question from each section. The fifth question may be attempted from any section. All questions carry equal marks.

SECTION—A

1. (a) Solve $x^2y \, dx - (x^3 - y^3) \, dy = 0$. 10
(b) Solve : $\cos^2x \, dy/dx + y = \tan x$. 10
2. Find the necessary and sufficient condition that the equation $Mdx + Ndy = 0$ (where M and N are functions of x and y with the condition that $\partial M/\partial y = \partial N/\partial x$ are continuous functions of x and y) may be exact. 20

SECTION—B

3. (a) Find the orthogonal trajectories of the family of conical circles $x^2 + y^2 + 2gx + c = 0$, g is parameter. 10
- (b) If $d^4y/dx^4 - 4y = 0$, show that
 $y = C_1 \cos(ax) + C_2 \sin(ax) + C_3 \cosh(ax) + C_4 \sinh(ax)$. 10
4. (a) Solve :
 $d^2y/dx^2 - 4dy/dx + 4y = 8(x^2 + e^{2x}) + \sin 2x$. 10
- (b) Show that the system of confocal conics
 $(x^2)/(a^2 + \lambda) + (y^2)/(b^2 + \lambda) = 1$ is self-orthogonal. 10

SECTION—C

5. (a) Obtain the primitive and singular solution (if it exists) of the equation $xp^2 - 2yp + 4x = 0$. 10
- (b) Solve and test for singular solution :
 $p^3 - 4xpy + 8y^2 = 0$. 10

6. (a) Solve : $x^2 \frac{d^2y}{dx^2} + 4x \frac{dy}{dx} + 2y = x + \sin x$.
10

(b) Solve :

$$(1+x)^2 \frac{d^2y}{dx^2} + (1+x) \frac{dy}{dx} + y = 4 \cos(\log(\sqrt{1+x})).$$

10

SECTION—D

7. (a) Solve : $x^2 \left(\frac{dy}{dx}\right)^2 - 2xy \left(\frac{dy}{dx}\right) + 2y^2 - x^2 = 0$.
10

(b) Solve: $4p^2x - (qx - k)^2 = 0$; k is parameter.
10

8. (a) Solve :

$$\frac{dx}{[x(y^2 - z^2)]} = \frac{dy}{y(z^2 - x^2)} = \frac{dz}{[z(x^2 - y^2)]}.$$

10

(b) Solve : $y'' + x^2y' = 1 + x + x^2$ in powers of x .

10